

1990-1991

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of order higher than in the time axis in the nonlinear interaction of the fundamental difficulties until a higher order in ϵ .

The nonlinear interaction of terms of various orders in ϵ does not prevent the possibility of justifying the

of two nearly tangent in the convergence of numerical calculations and are worth

The axisymmetric motions

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When they are solved, it is found that the pressure functions have asymptotic behavior for large R as follows:

$$140(1+\lambda)^2$$

$$P \propto R^{-4} + O(R^{-6}), \quad \tau \propto R^{-2} + O(R^{-4})$$

TABLE I. Revised convergence properties of series for $X_{\alpha\beta}^M$. The columns compare the convergence of infinite series expansions that do not use the $\xi \ln \xi$ terms obtained here with ones that do. The improvement in the convergence with the number of terms n is clear.

	M_{11}^M		M_{22}^M	
	without $\xi \ln \xi$ terms	with $\xi \ln \xi$ terms	without $\xi \ln \xi$ terms	with $\xi \ln \xi$ terms
$n=100$	0.719 27	0.716 80	-0.141 94	-0.145 52
$n=200$	0.718 58	0.717 33	-0.144 24	-0.145 98
$n=300$	0.718 15	0.717 31	-0.144 80	-0.145 97
$n=400$	0.718 05	0.717 30	-0.144 80	-0.145 97

$$X_{11}^M = \frac{\epsilon^{-1}}{265} + \frac{1}{200} \ln \xi^{-1} + 0.717175 + \frac{353}{2800} \xi \ln \xi^{-1} + 0.07\xi, \quad (17)$$

$$X_{22}^M = \lambda \epsilon^{-1} + \frac{27}{100} \ln \epsilon^{-1} - 0.1460 + \frac{493}{2800} \xi \ln \xi^{-1} + 0.15\xi, \quad (18)$$

where $\epsilon = \epsilon$ when $\lambda = 1$. As further tests of the new results,

the convergence tests of Jeffrey and Saffman⁶² and Jeffrey and Saffman⁶³ were done again. Some results are shown in Table I. It can be seen that the convergence is improved using the new values.

$$477 = 651^4 + 8322^3 - 10412^2 + 9881 - 660$$

at rest in an ambient rate-of-strain field,⁴ we expect the

the coefficients, we $G_{\alpha\beta}$ functions, but incor- corrected expressions for

⁶²D. J. Jeffrey and J. Saffman, *J. Fluid Mech.* **192**, 487 (1979).
⁶³R. M. Corless and D. J. Jeffrey, *J. Appl. Math. Phys.* **39**, 874 (1988).
⁶⁴J. Happel and H. Brenner, *Low Reynolds Number Hydrodynamics* (Nijhoff, The Hague, The Netherlands, 1983).
⁶⁵D. J. Jeffrey, *Utilitas Math.* (in press).

we see that they were correct for the $X_{\alpha\beta}^M$ functions. The $\lambda = 1$ are