

# An Algebraic Method for Analyzing Open-Loop Dynamic Systems

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Abstract. This paper describes an algebraic method for analyzing open-loop dynamic systems. The method is implemented in the Maple computer algebra system using the Dynaflex and RifSimp packages.

Keywords. Algebraic method, open-loop dynamic systems, Maple, Dynaflex, RifSimp, Dynaflex, RifSimp.



such as a four-bar mechanism, in which the components connect back to the structure being considered.

When a structure forms a closed loop, then Dynaflex will generate constraint equations that describe the drop in the degrees of freedom that accompanies the closing of a loop. From the point of view of this paper, we have discovered that the RifSimp package takes a great deal of time and memory to analyze closed-loop systems, but can make good progress with open-loop ones. This is what is reported here.

## 2 Example System Analysed Using Dynaflex

In order to keep the examples within printable limits, we shall use a simple spinning top as an example. A top is an axisymmetric body that spins about its body-fixed symmetry axis. It can precess about a vertical ( $Z$ ) axis, and nutate about the rotated  $X$  axis. Figure 1 shows gravity acting in the  $-Z$  direction. The center of mass is located at  $C$ , and the spinning top is assumed to rotate without slipping on the ground; this connection is modelled by a spherical (ball-and-socket) joint at  $O$ . The joint coordinates at  $O$  are represented by Euler angles  $(\alpha, \beta, \gamma)$ , in the form of 3-1-3 Euler angles, meaning that they correspond to precession, nutation, and spin, respectively.

### 2.1 The System Graph

The system graph for the top is shown in Figure 2. The graph consists of nodes and edges. The nodes correspond to centres of coordinates, while the edges describe the system. Thus in the figure, we see nodes







4. - 2. 3. 4.

## 5 Some Special Cases

The importance of the

